

# ADELA 2016 - COLOMBIA

## Co-location satellite GPS and SLR geodetic techniques at the Felix Aguilar Astronomical Observatory of San Juan, Argentina

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F. Podestá , E. Albornoz , A. Navarro y M. Luna



This presentation shows the strategy followed to get the mathematical co-locations between SLR telescope and permanent station GPS antenna, in the Felix Aguilar Astronomical Observatory of San Juan, Argentina

The work allows the coordinates of the Station can be obtained by combining data from both techniques and greater level of accuracy than each individually.

The IERS considers stations co-localized as the points more valuable and important for maintaining the Terrestrial and Celestial Reference Systems.

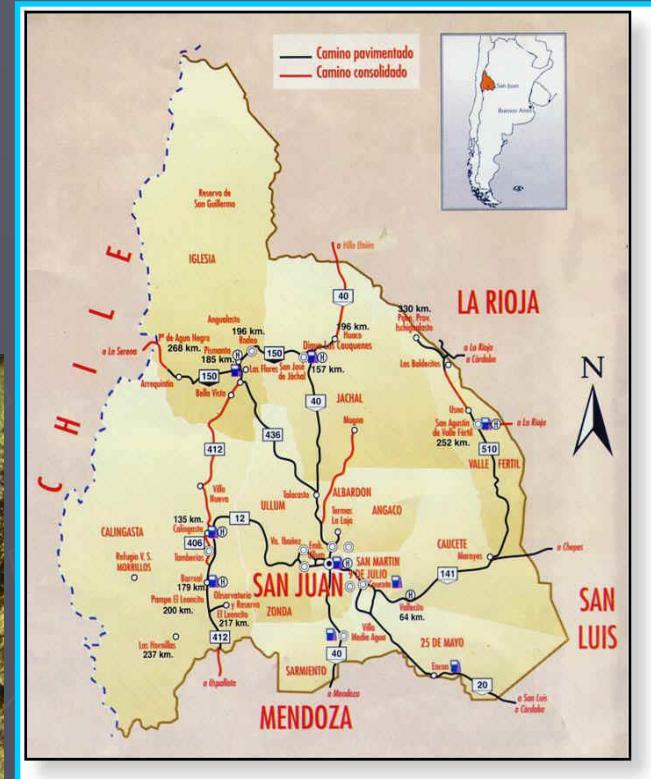
# SAN JUAN - ARGENTINA

Surface: 89.651 Km<sup>2</sup>

Population: 700000 people

Density: 7 people / Km<sup>2</sup>

Weather: Sunny and Dry



**Félix Aguilar  
Astronomical  
Observatory**

## System and Frame References

- Reference System (RS) is a geometric structure that serves to refer the coordinates of points in space. It can be defined by three axes with its origin and directions, scales, algorithms spatial-temporary transformations and constant.
- Reference Frame (RF) is the SR materialization. It is a group of element that determine accurately the SR and is constructed by the coordinates of the points of definition (observatories), applied techniques and methods of calculation

In Astronomy, Geodesy and Geodynamics two fundamental  
**RS and RF are necessary**

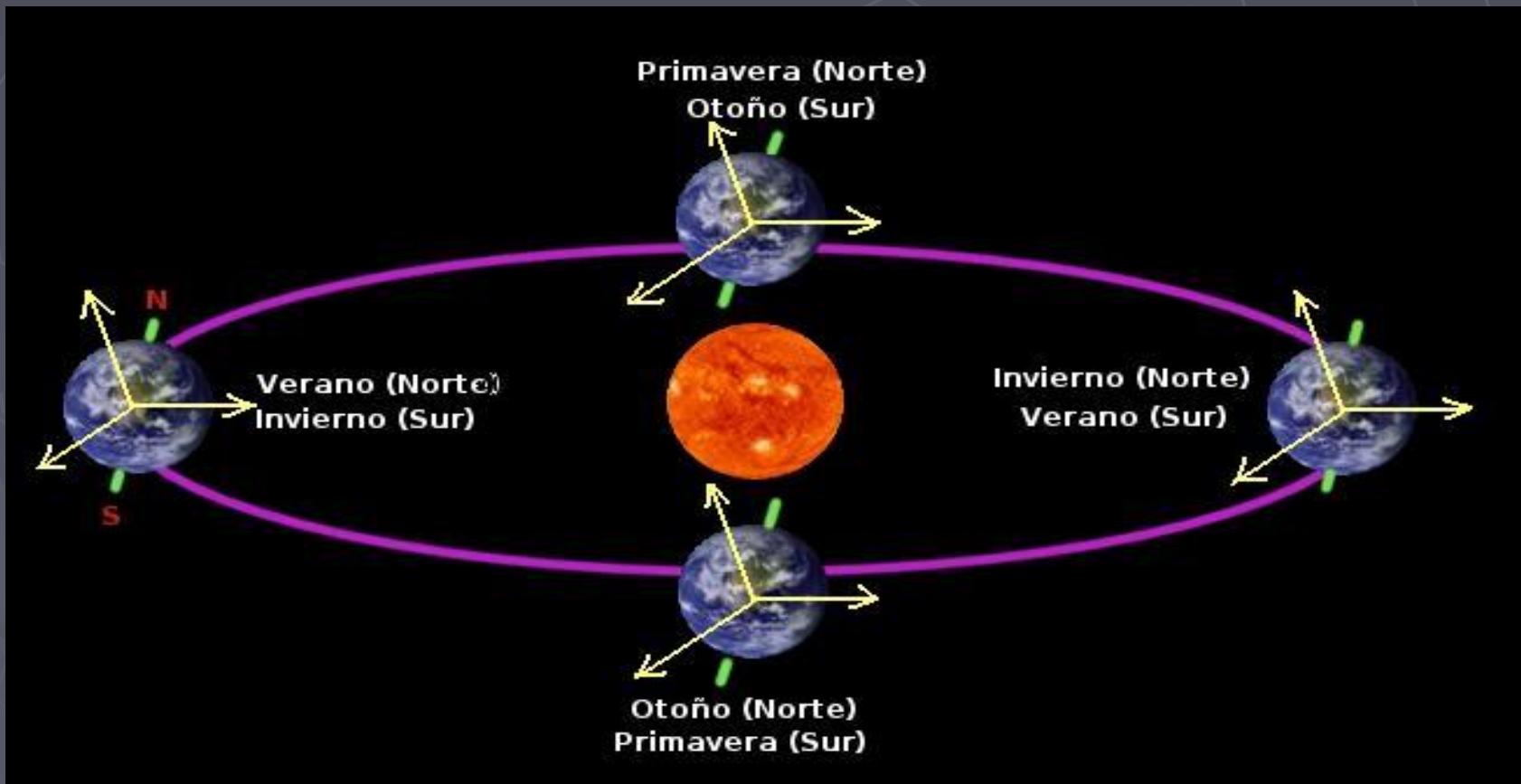
**CELESTIAL**



**TERRESTRIAL**

Inertial Systems: A body persists in resting state or uniform rectilinear movement to unless an applicant force change their status

Quasi Inertial System: NO rotating system based on classical mechanics.  
Its origin can be accelerated



The Earth geocenter moves around an ellipse, while its axis is always parallel to themselves

Assembly Year 2000

International Geodesy and Geophysics Union (IGGU)  
International Astronomical Union (IAU)

Modification of traditional and ancestral definitions from **01/01/2003**

New definitions to Celestial and Terrestrial RS. An **Intermediate System** appears

**New concepts**

Celestial Intermediate Pole (CIP)

Changes in Precession-Nutation theory (PN)

Celestial Intermediate Origin (CIO)

Terrestrial Intermediate Origin (TIO)

Earth Rotation Angle (ERA)

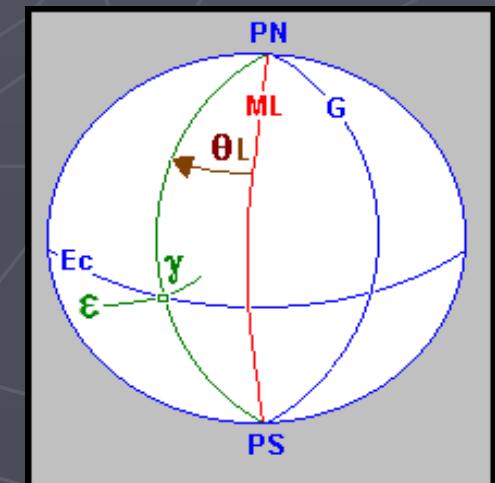
Vernal Point or Equinox

Ecliptical Plane

Sideral Time

Greenwich Meridian

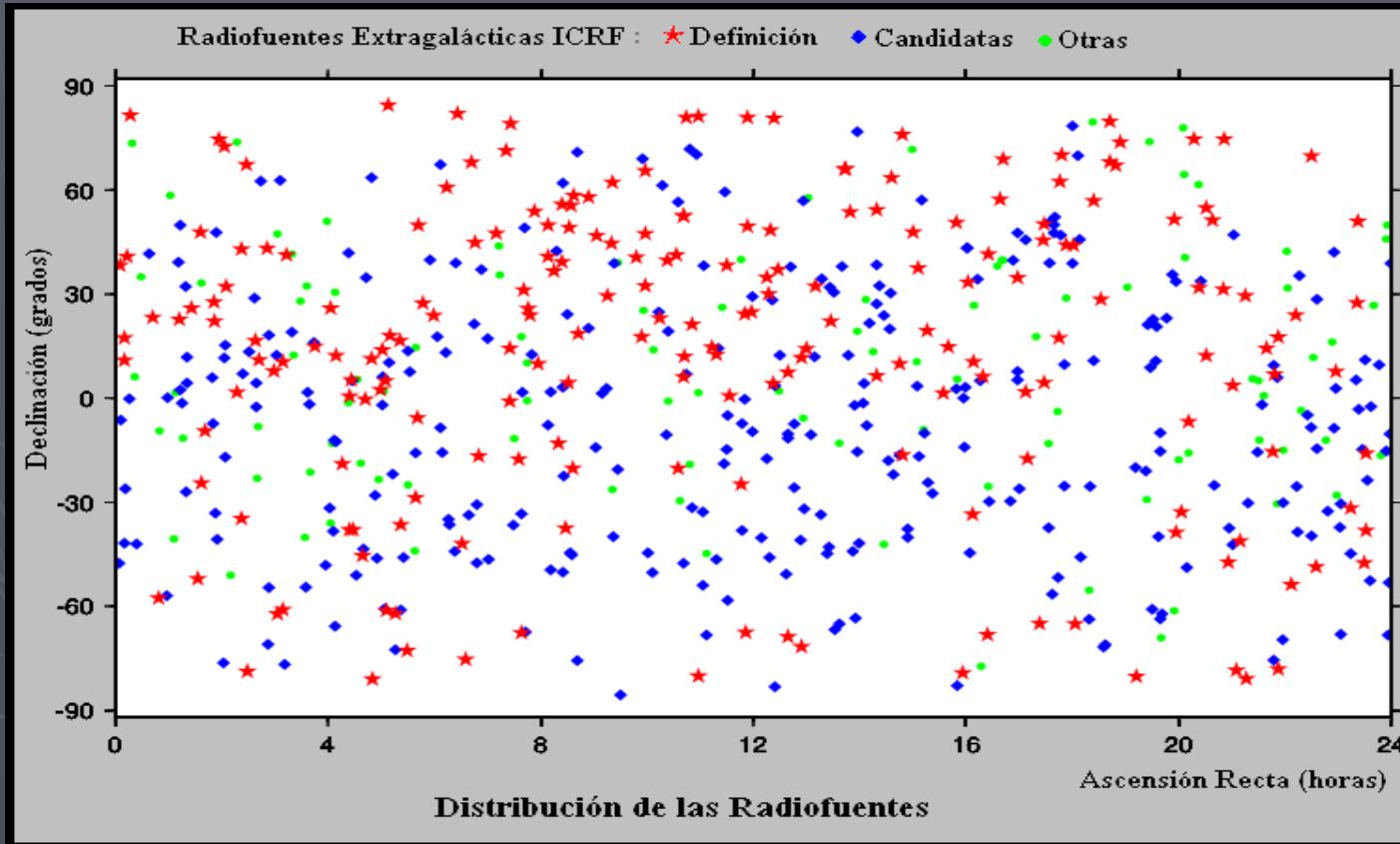
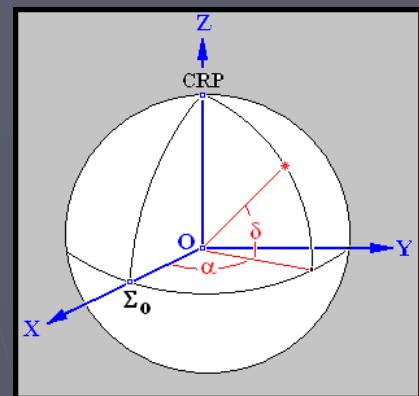
**Obsoletes concepts**



RS →

Celestial Baricentrical (BCRS)

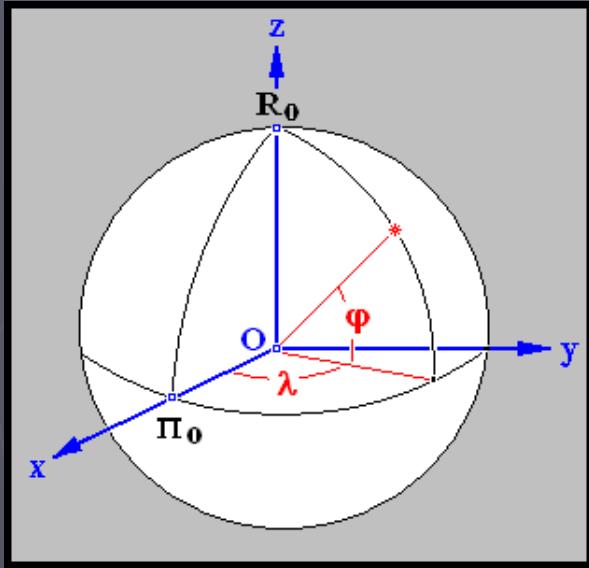
Celestial Geocentrical (GCRS)



International  
Celestial  
Reference  
Frame  
(ICRF)

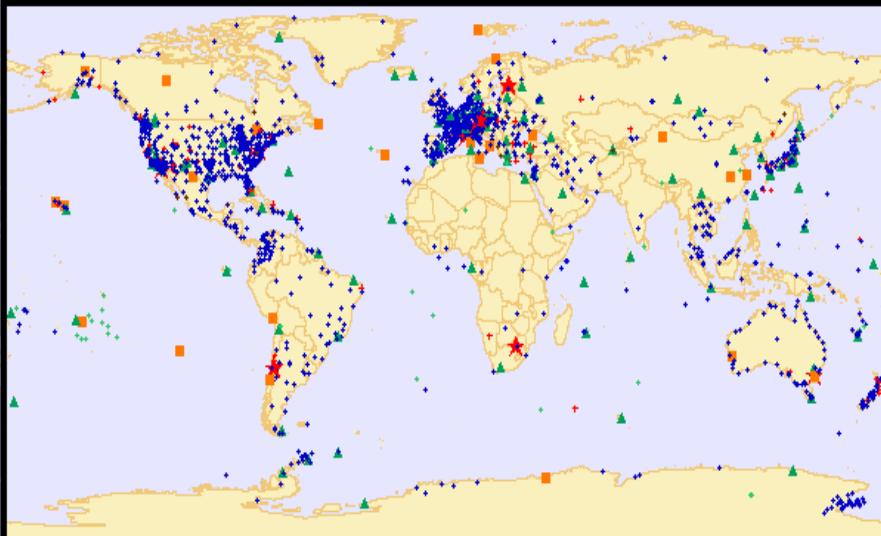
- Coordinates J2000.0 with VLBI of 900 Radio-sources IERS ( more 300 definition )
- Mili arc second precision
- Origin Baricentric of the Solar System + General Relativity

## International Terrestrial Reference System (ITRS)



- \* Accompanies the rotation of the Earth
- \* Gives the position and velocity of a point on the surface
- \* The variations are due to geophysical causes
- \* The RF associated is formed by the coordinates geodesic Stationsl

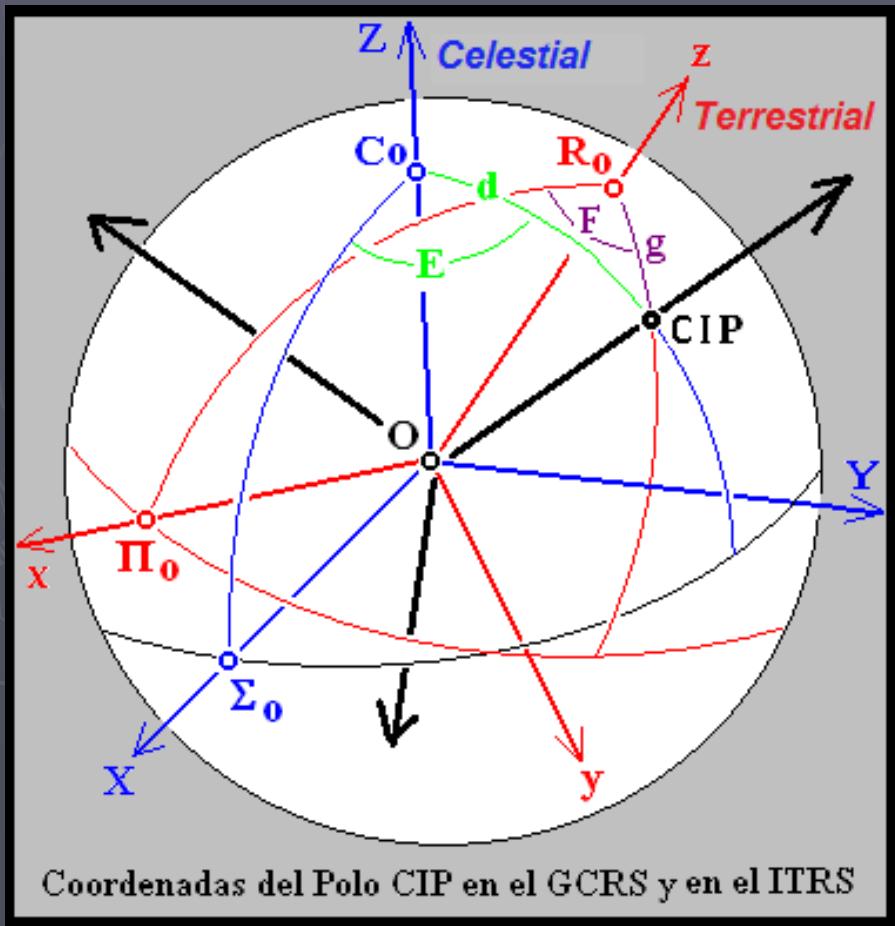
## International Terrestrial Reference Frame (ITRF)



- \* Net Stations VLBI, LLR, SLR, GPS and Doris.
- \* Set of Coordinated and Velocity of IERS Stations (epoch ITRF yy)
- \* Each Station produces particular RF and IERS give the final ITRF

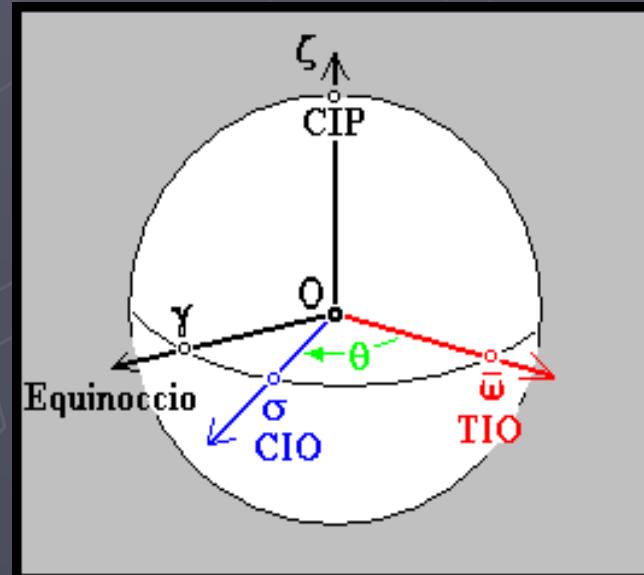
# New Definitions to Origins

## Celestial Intermediate Pole (CIP)



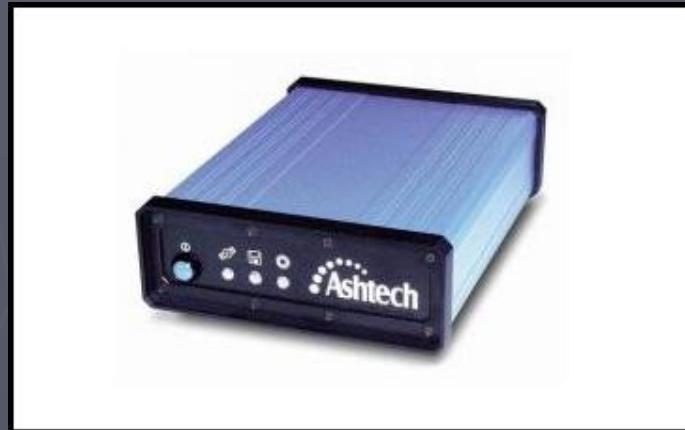
Assembly UAI 2000  
From date 01/01/2003

Celestial Intermediate Origin (CIO)  
Terrestrial Intermediate Origin (TIO)

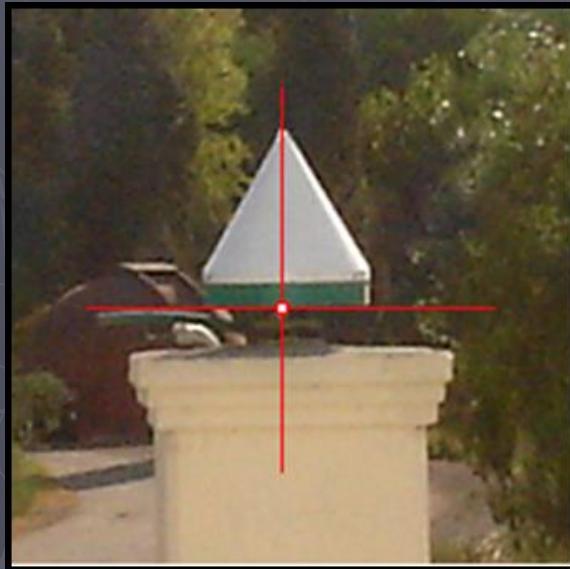


$$\theta = \text{arc } \omega \sigma$$

# GPS Permanent Station



**ASHTECH - Micro Z-CGRS**



**Reference point**



**Pillar with GPS antenna**

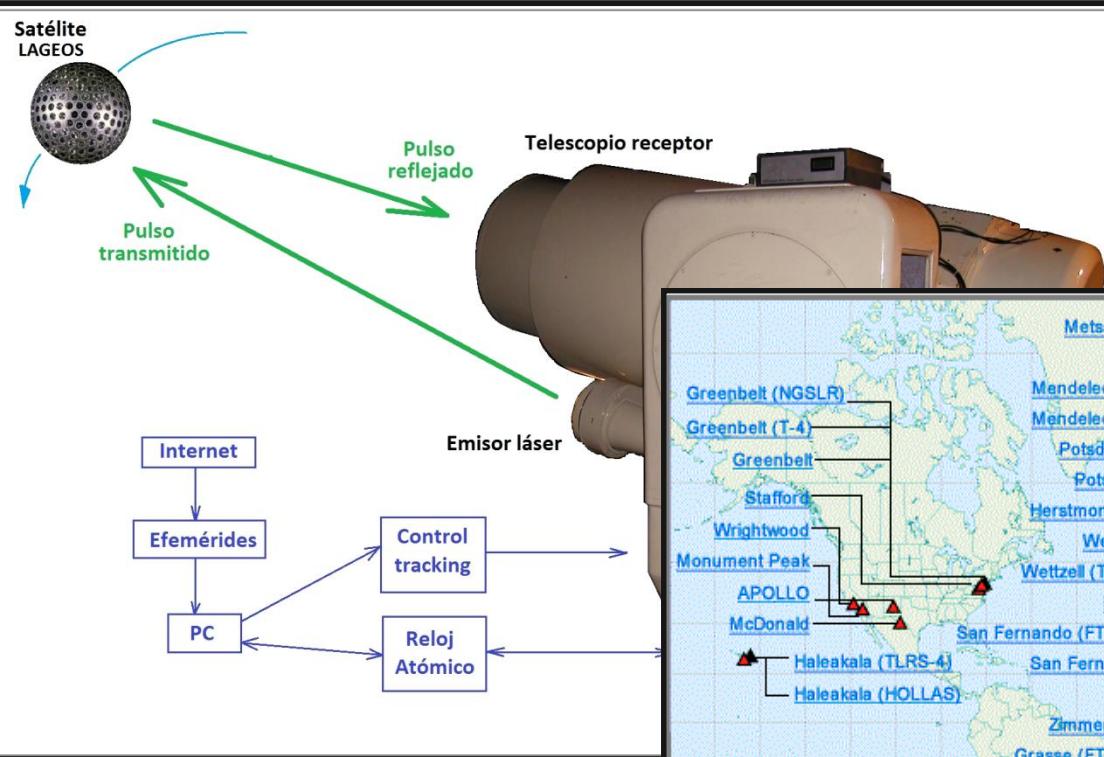


**Edificio Walter T. Manrique**

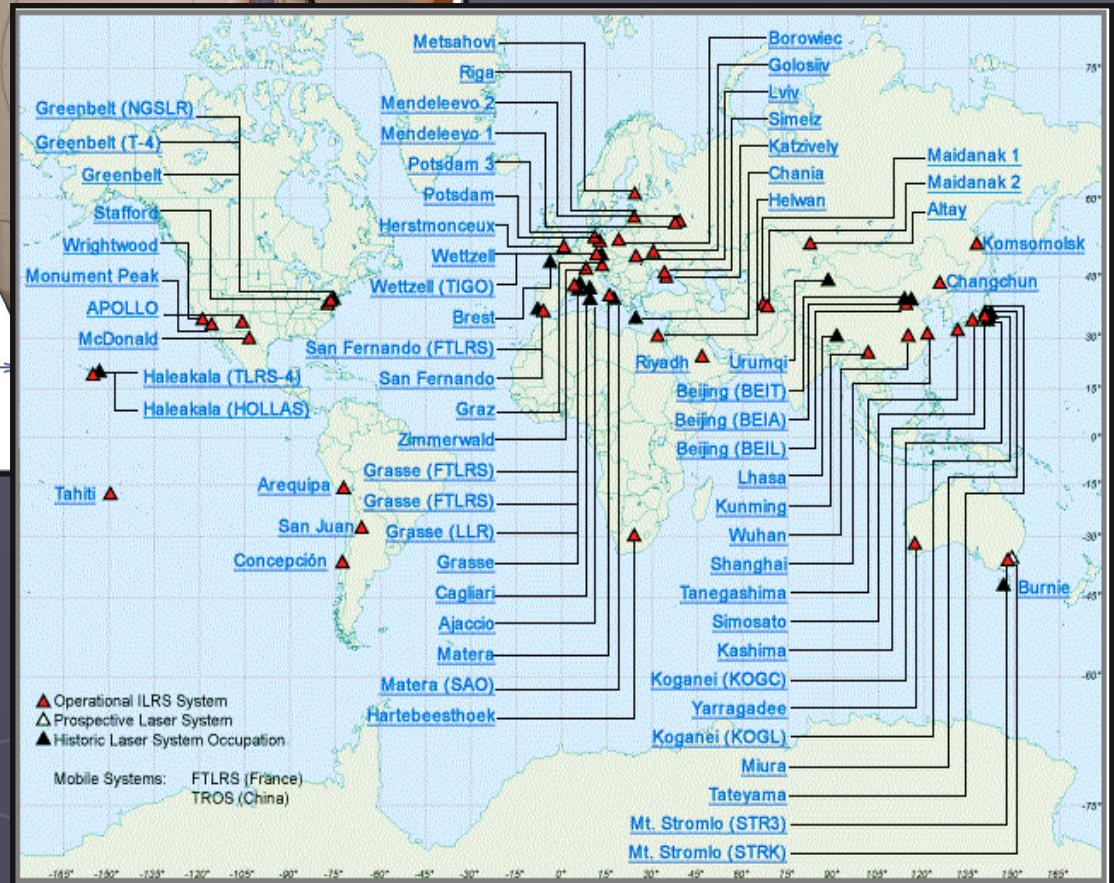


**Punto de referencia**

# Satellite Laser Ranging (SLR)



Operating Scheme



ILRS Net Global

International Laser Ranging  
Service

# SLR System in OAFA

## Place

X = 1984104.114 m

Y = -5068867.289 m

Z = -3314482.433 m

L = -31°.5086249

B = -68°.6231602

H = 727.221 m



Cassegrain Telescope

Aperture 0.60 [m]

Mont AZ - EL

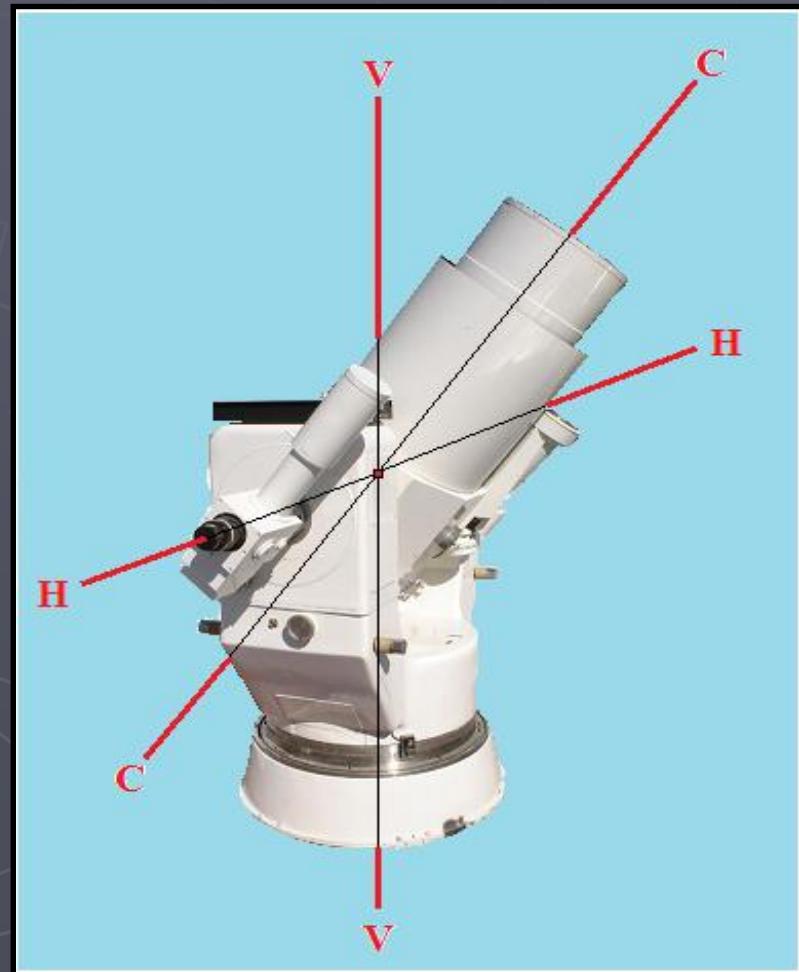
Oscillator Nd: YAG

**Primary Wavelength 1064 [nm]**

Máx. Energy 80 [mJ ]

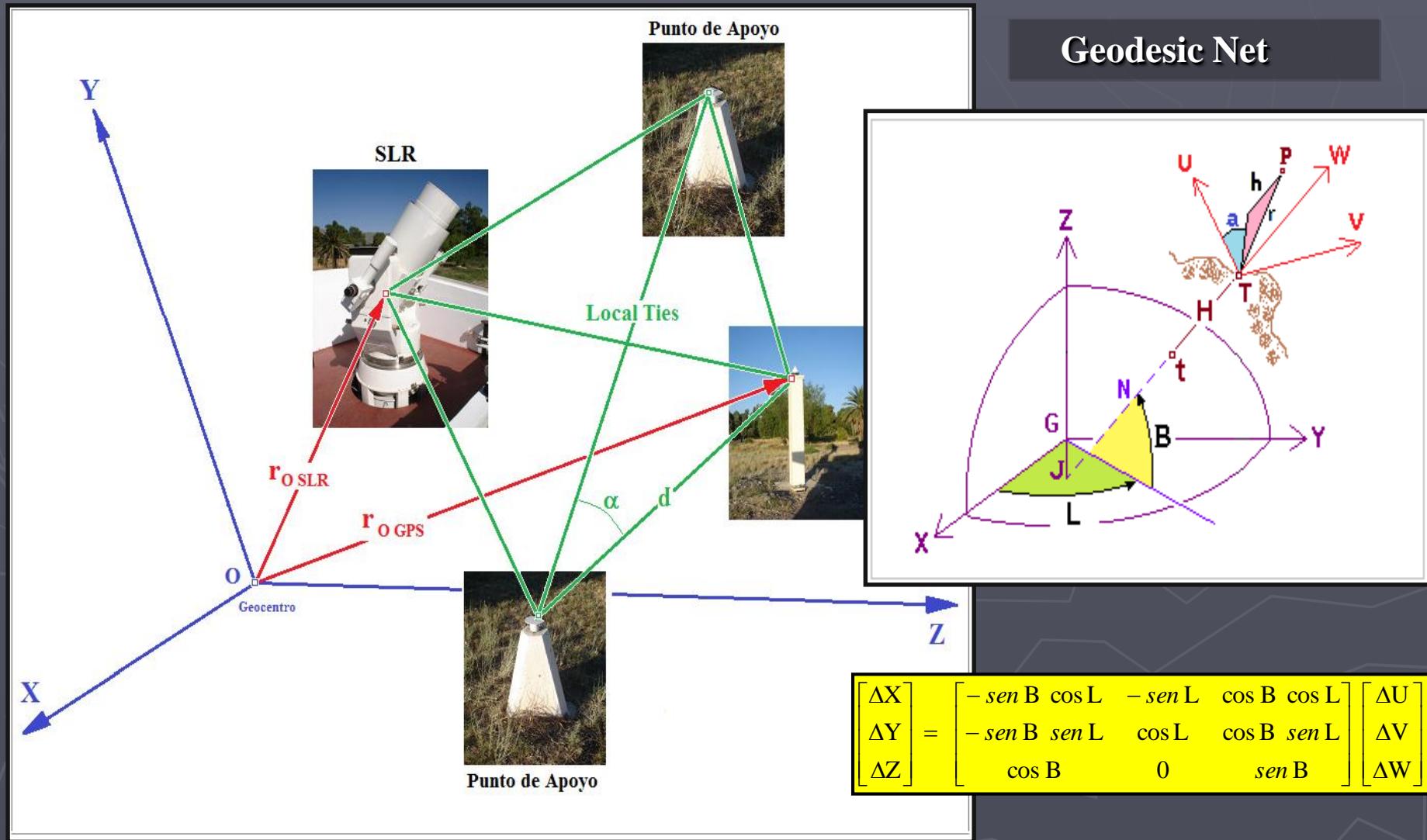
**Secundary Wavelength 532 [nm]**

Pulse width 30-50 [ps]



## Co-localización Definición - Local Ties LT

Co-localization site is defined by two or more space geodetic techniques occupying nearby, linked to each other with very precise measurements in 3D



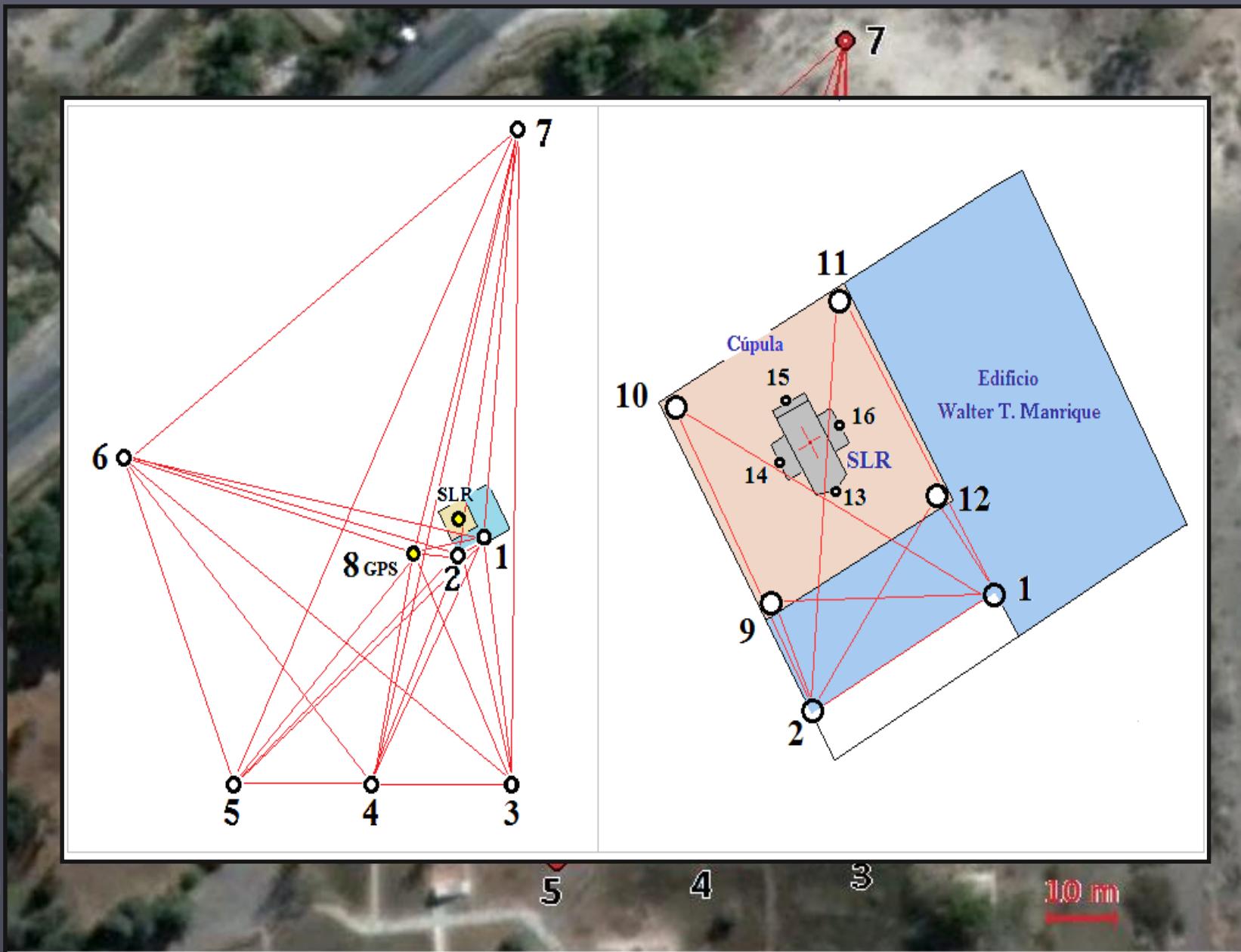


GPS geodésic TRIMBLE



GPS GTR-A

# Geodesy Net



## Set up of the reference points

Point 7



Point 3

Points 1 y 2

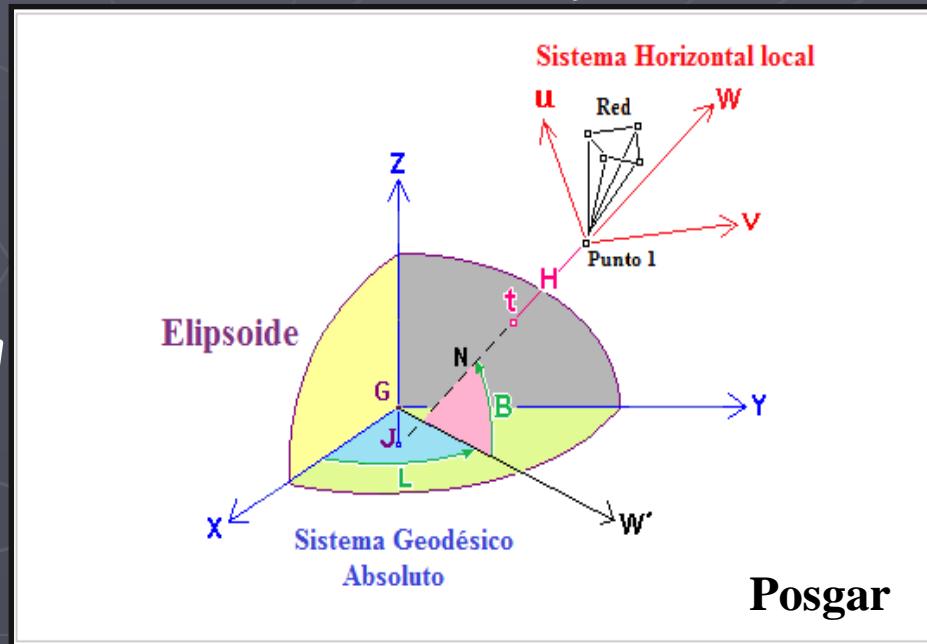
## Metodology

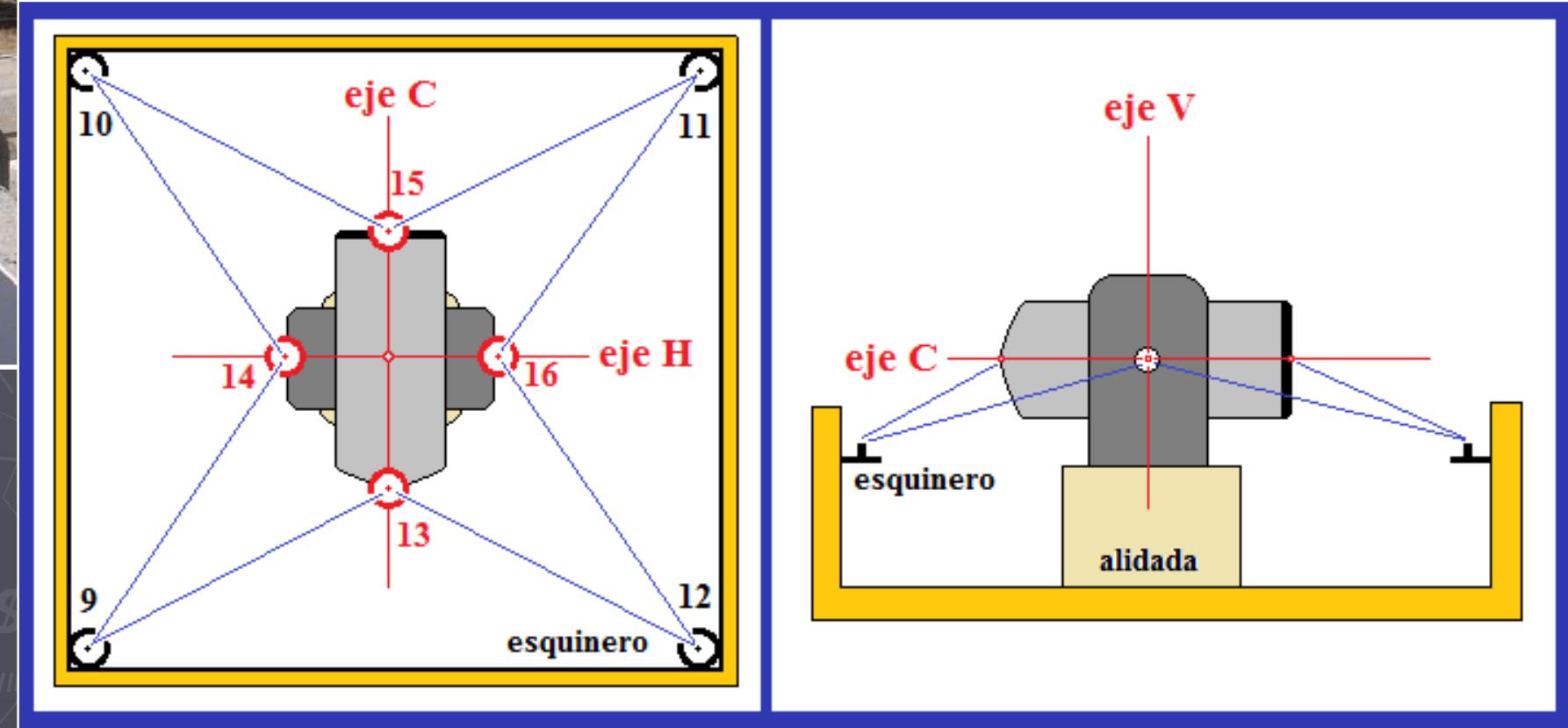
Tradicional Net  
in a local system

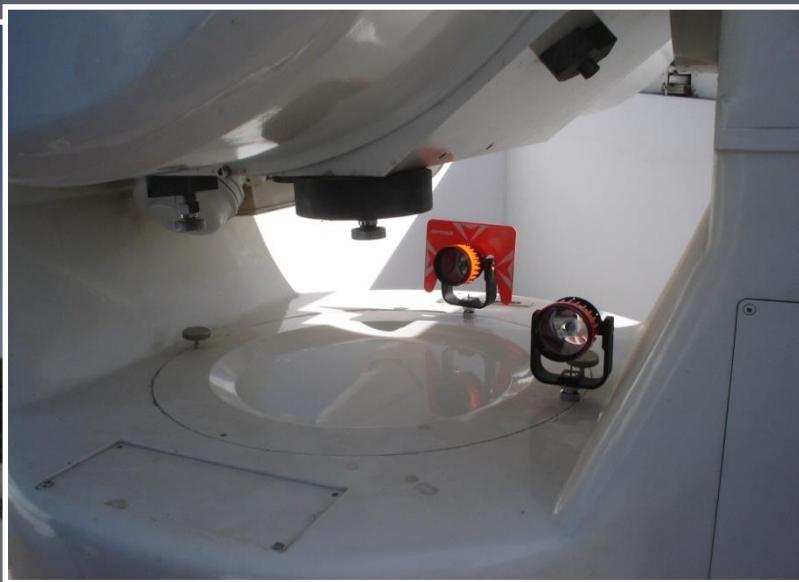
GPS Net  
in a local system

Measure of angles and distances  
Trilateration and Leveling

Vectors determination







# Calculation and compensation

## Output file REDGPS\_ALV with the matrix Variance – Covariance of the observed vectors components

Matriz OGPS

Punto Origen / Punto Extremo / dx / dy / dz

6.0000	5.0000	2.2740	31.6120	-45.3680
6.0000	7.0000	79.4790	-17.6240	73.6150
6.0000	7.0000	79.4770	-17.6300	73.6190
6.0000	3.0000	46.9970	49.0400	-45.2550
5.0000	7.0000	77.2050	-49.2340	118.9810
5.0000	3.0000	44.7260	17.4260	0.1130
.....				
.....				

Punto Origen-Punto Extremo

1.0e-004 \*

6-5

0.1330	0	0
-0.0770	0.3150	0
0.0043	0.0061	0.0963

6-7

0.1820	0	0
-0.1070	0.2980	0
-0.0127	0.0077	0.0920

6-3

0.2280	0	0
-0.1290	0.5730	0
0.0066	0.0129	0.1680

...

\*PASA EL TEST CHI CUADRADO AL 95%\*

\*COORDENADAS AJUSTADAS\*

PUNTO	X	Y	Z
1.00	1984110.41	-5068864.32	-3314482.44
2.00	1984106.39	-5068864.51	-3314484.58
3.00	1984100.26	-5068831.66	-3314531.04
4.00	1984077.89	-5068840.38	-3314531.10
5.00	1984055.53	-5068849.09	-3314531.15
6.00	1984053.25	-5068880.70	-3314485.78
7.00	1984132.73	-5068898.33	-3314412.17
8.00	1984095.78	-5068868.33	-3314485.50

\*ERRORES ESTANDAR DE LAS COORDENADAS AJUSTADAS\*

PUNTO	ERRX.	ERRY.	ERRZ.	EERM(est.)
1.0000	0.0005	0.0007	0.0005	0.0009
2.0000	0.0006	0.0008	0.0007	0.0012
3.0000	0.0005	0.0007	0.0005	0.0010
4.0000	0.0005	0.0007	0.0005	0.0010
5.0000	0.0005	0.0006	0.0005	0.0009
6.0000	0.0005	0.0007	0.0005	0.0010
7.0000	0.0005	0.0007	0.0004	0.0009
8.0000	0.0004	0.0006	0.0004	0.0009

# Error Ellipses

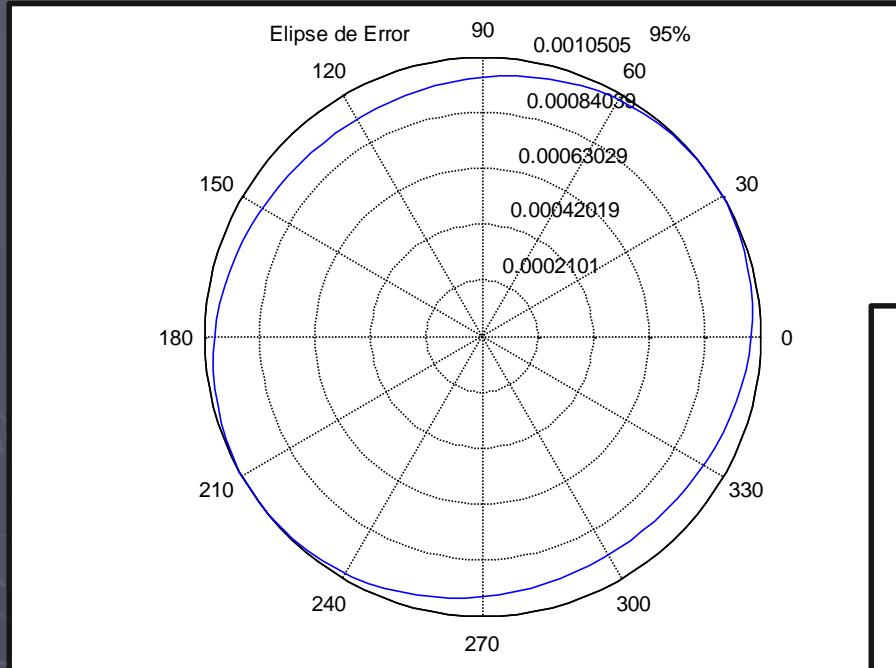
**\*ELIPSE PUNTO\* 1**

**\*SEMIEJE MAYOR A=0.0011 m ,**

**\*SEMIEJE MENOR B=0.0009 m**

**\*AZIMUT FI=34.83 grados ,**

**\*EXCENT.=0.1881 , \*AREA (cm<sup>2</sup>) = 0.03**



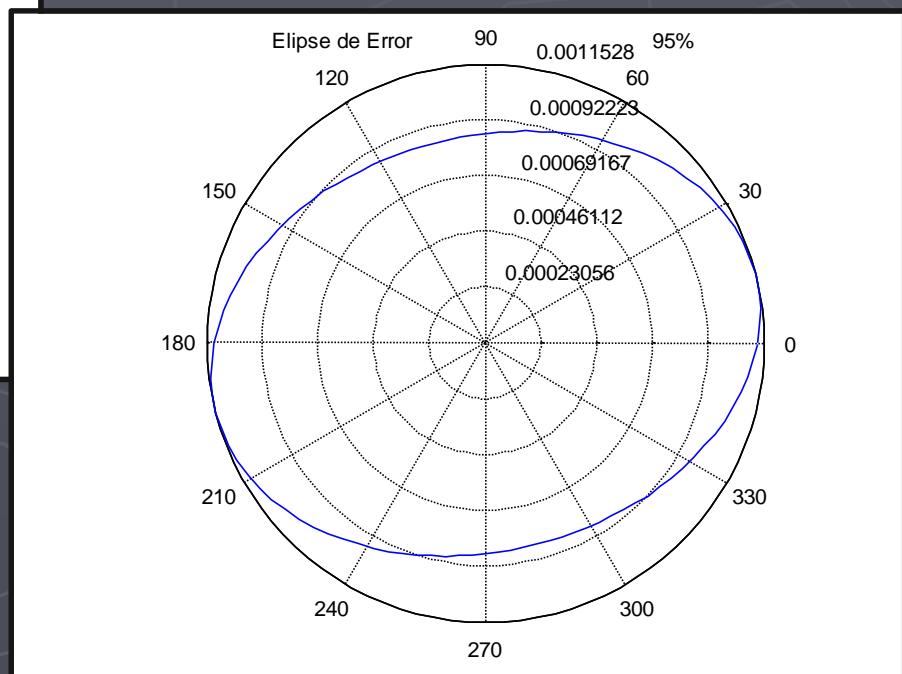
**\*ELIPSE PUNTO\* 7**

**\*SEMIEJE MAYOR A=0.0012 m ,**

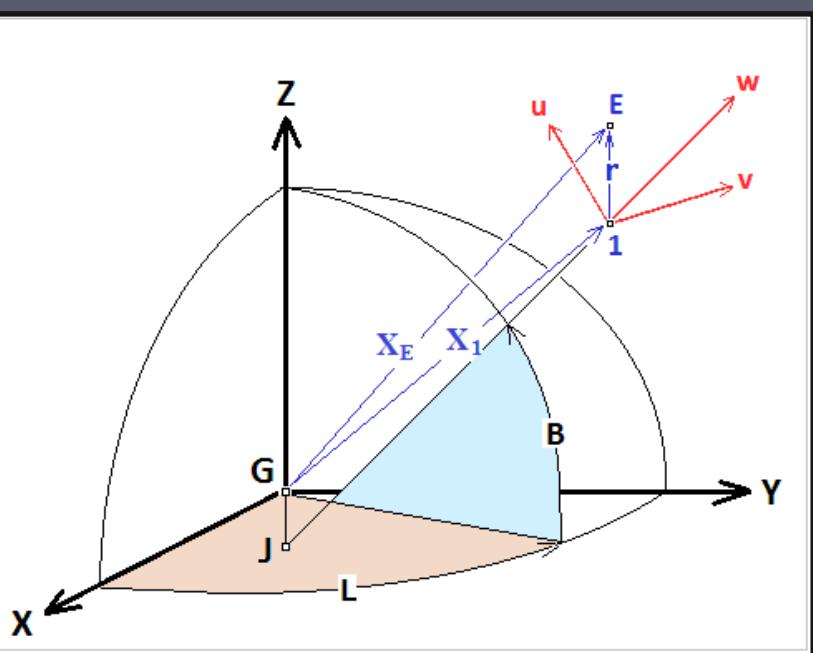
**\*SEMIEJE MENOR B=0.0009 m**

**\*AZIMUT FI=14.54 grados ,**

**\*EXCENT.=0.4456 , \*AREA (cm<sup>2</sup>) = 0.03**

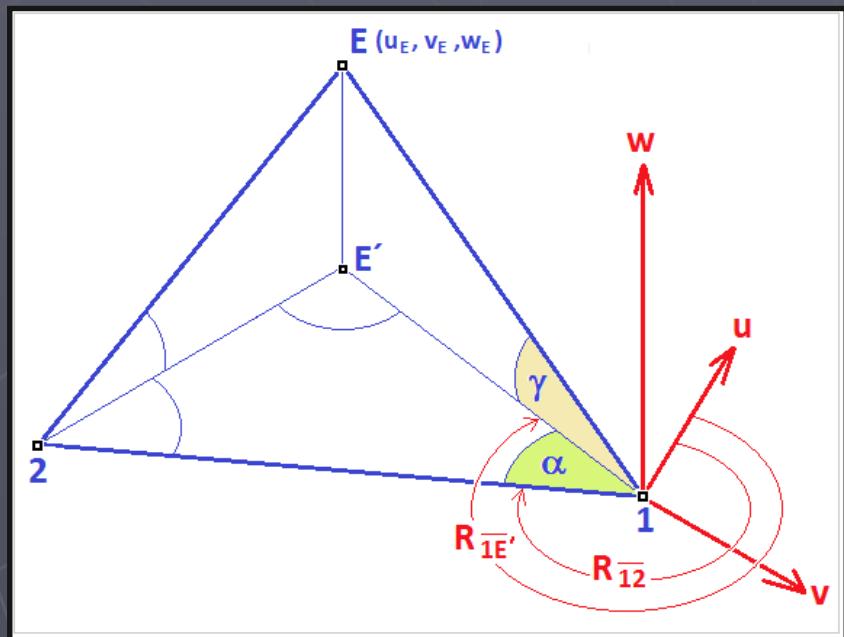


## Error propagation



$$\sigma_{w_E} = \sqrt{\left(\frac{\partial f}{\partial \bar{1E}}\right)^2 \sigma_{\bar{1E}}^2 + \left(\frac{\partial f}{\partial \gamma}\right)^2 \frac{\sigma_\gamma^2}{206265^2}}$$

Based on the local system centered on the vertex 1 of the geodetic network, errors propagated by the linear and angular measurements cornerbacks points are determined by the formulas:



$$\sigma_{u_E} = \sqrt{\left(\frac{\partial f}{\partial \bar{1E}}\right)^2 \sigma_{\bar{1E}}^2 + \left(\frac{\partial f}{\partial \alpha}\right)^2 \frac{\sigma_\alpha^2}{206265^2} + \left(\frac{\partial f}{\partial \gamma}\right)^2 \frac{\sigma_\gamma^2}{206265^2} + \left(\frac{\partial f}{\partial R_{\bar{12}}}\right)^2 \frac{\sigma_{R_{\bar{12}}}^2}{206265^2}}$$

$$\sigma_{v_E} = \sqrt{\left(\frac{\partial f}{\partial \bar{1E}}\right)^2 \sigma_{\bar{1E}}^2 + \left(\frac{\partial f}{\partial \alpha}\right)^2 \frac{\sigma_\alpha^2}{206265^2} + \left(\frac{\partial f}{\partial \gamma}\right)^2 \frac{\sigma_\gamma^2}{206265^2} + \left(\frac{\partial f}{\partial R_{\bar{12}}}\right)^2 \frac{\sigma_{R_{\bar{12}}}^2}{206265^2}}$$

## Final coordinates of the network points

Posgar 2007, epoch June 26/2012 (2012.403).

Punto	X	Y	Z
1	1984110,4081	-5068864,3161	-3314482,4443
2	1984106,3887	-5068864,5135	-3314484,5838
3	1984100,2568	-5068831,6577	-3314531,0416
4	1984077,8903	-5068840,3763	-3314531,1024
5	1984055,5276	-5068849,0898	-3314531,1517
6	1984053,2547	-5068880,6993	-3314485,7836
7	1984132,7308	-5068898,3303	-3314412,1670
8	1984095,7826	-5068868,3277	-3314485,5004
9	1984105,4952	-5068866,0664	-3314482,3068
10	1984104,1382	-5068868,7369	-3314479,3020
11	1984107,6748	-5068868,1806	-3314477,1238
12	1984109,0978	-5068865,6022	-3314480,1866
CGL	1984106,7928	-5068867,4829	-3314479,9346

$$\text{Vector Punto 8 - CGL} = \sqrt{(X_8 - X_{\text{CGL}})^2 + (Y_8 - Y_{\text{CGL}})^2 + (Z_8 - Z_{\text{CGL}})^2} = 12.3659 \text{ metros}$$

## Standard errors of the adjusted coordinates (meters)

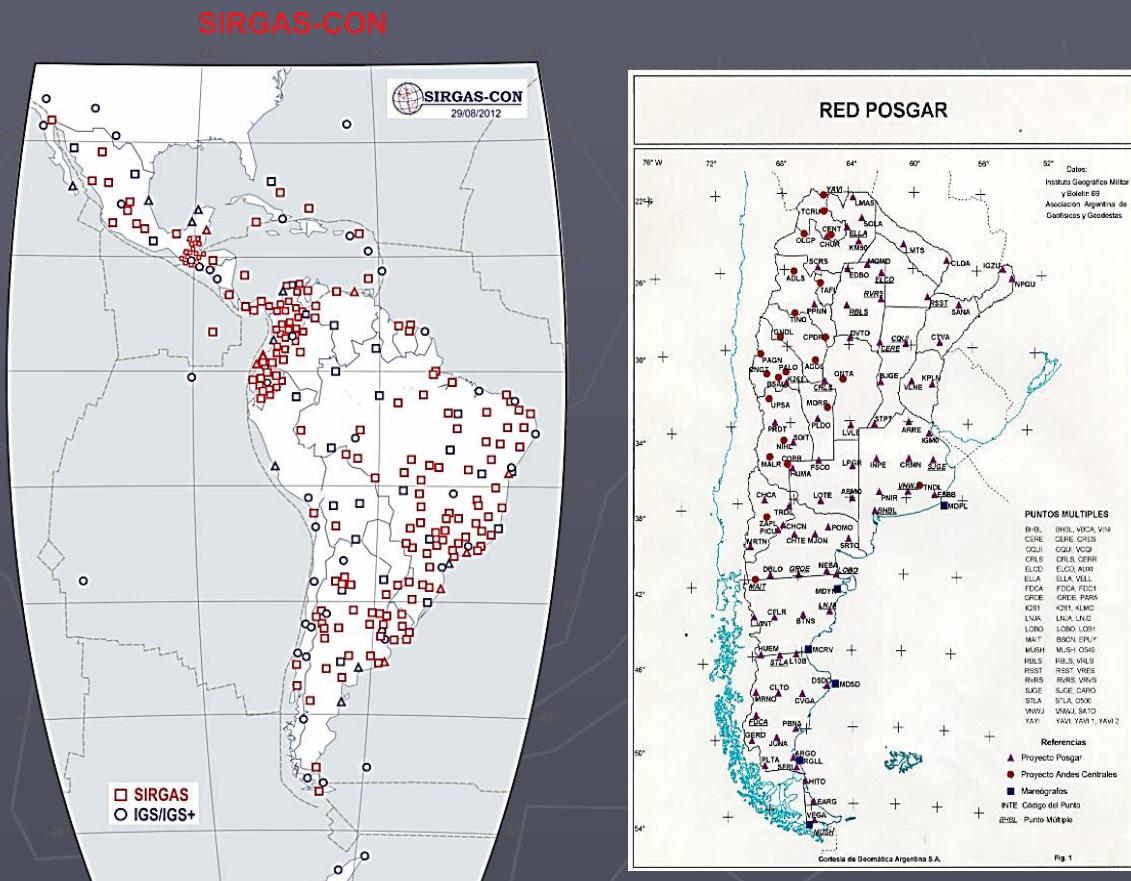
Punto	sX	sY	sZ
1	0,0005	0,0007	0,0005
2	0,0006	0,0008	0,0007
3	0,0005	0,0007	0,0005
4	0,0005	0,0007	0,0005
5	0,0005	0,0006	0,0005
6	0,0005	0,0007	0,0005
7	0,0005	0,0007	0,0004
8	0,0004	0,0006	0,0004
9	0,0015	0,0011	0,0023
10	0,0014	0,0016	0,0022
11	0,0010	0,0024	0,0016
12	0,0011	0,0023	0,0016
CGL	0,0010	0,0031	0,0014

# Conclusions

Space geodetic techniques are only used in the development of frameworks.

Addition to the primary core ITRF observation stations, the global network is densified with regional GPS subnets. In America and in Argentina densification SIRGAS and POSGAR have positions within the centimeter accuracies and speeds of the order of 1.5 mm / year.

A station acquires status station co-located, you can integrate these networks as a reference of the first order



**The network designed did not consider the location of any point east of the building Walter Manrique. Despite this adjustment was excellent but, in order to provide the network with greater strength, it would be advantageous densify with a vertex to the east with direct visibility point 1.**



**Due to the impossibility of view between the terrestrial network points and mount SLR, we had to designing a particular methodology for connection**

Obviously there are propagation of errors in the coordinates due to linear and angular measurements taken.

The average standard deviations in all three axes increased from external points (1 to 8) to internal (9 to CGL); but everything indicates that worked very carefully, because the resulting error in determining the CGL is within the requirements of the IERS.

The standard deviations of the rectangular geodetic coordinates obtained in the adjustment of all network points were within 3 mm, excelling value that will enable the OAFA to be considered by the IERS as a co-located station.





**MUCHAS GRACIAS**